

Concerning the Stand-Off Distance of the Bow Shock

D. G. Sibeck¹ and M. V. D. Silveira²

¹Heliophysics Division, NASA/GSFC, Greenbelt, MD 20771

²University of Sao Paulo-Lorena School of Engineering, Lorena, Brazil

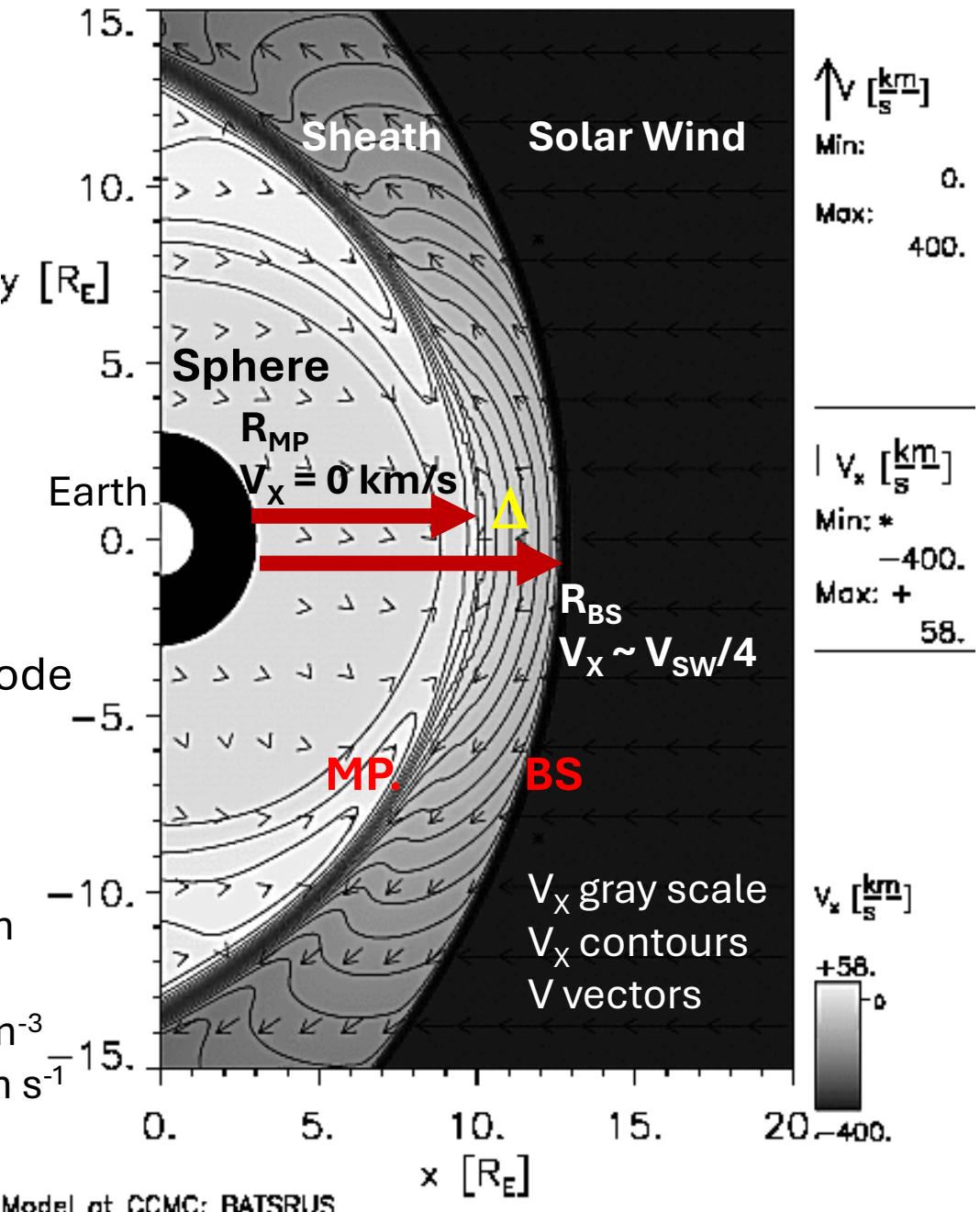
Outline

- Bow shock and magnetopause definitions
- What use is a standoff distance?
- Past empirical studies
- The new velocity gradient method
- Initial results
- Conclusion

Bow Shock and Magnetopause Definitions

- At rest, the magnetopause lies along the locus of points where magnetosheath & magnetospheric pressures balance. At subsolar MP $\rightarrow V_x = 0$
- At rest, the bow shock lies upstream from the magnetopause along the locus of points where fast mode wave speeds match incoming solar wind velocities. At subsolar BS $\rightarrow V_x = V_{sw}/4$ (for large Mach numbers)
- The stand-off distance $\Delta = R_{BS} - R_{MP}$

U. Michigan
BATS-R-US
 $N = 6.25 \text{ cm}^{-3}$
 $V = -400 \text{ km s}^{-1}$
 $T = 2 \times 10^5 \text{ K}$
 $B_z = 5 \text{ nT}$



The Standoff Distance to the Bow Shock

- In gasdynamics, the standoff distance to the subsolar bow shock from the subsolar magnetopause is given by:

$$\Delta = R_{BS} - R_{MP} = R_{MP} * (1.1 * (\gamma - 1) M_s^2 + 2) / [(\gamma + 1) * M_s^2]$$

- And empirical gasdynamic studies indicate that

$$\Delta = 1.1 R_{MP} * V_{SHEATH} / V_{SW} = 1.1 R_{MP} * \rho_{SW} / \rho_{SHEATH}$$

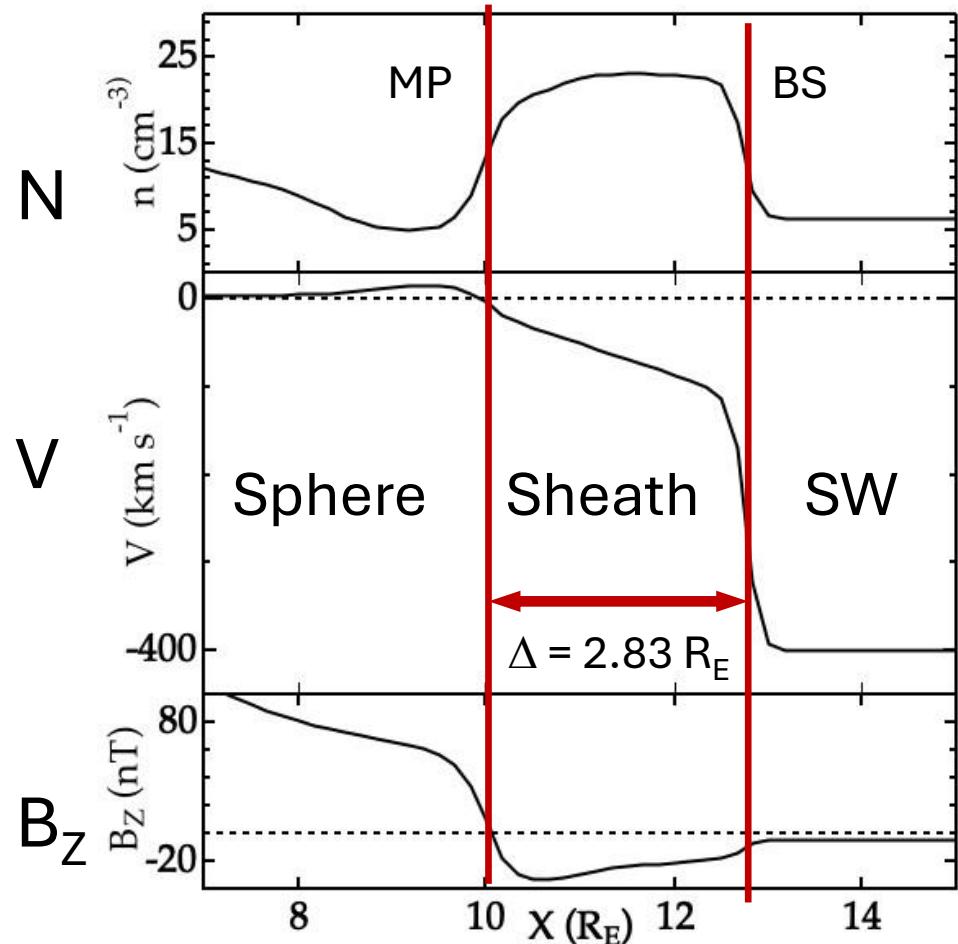
...depends on sonic Mach number M_s (known) and ratio of specific heats or adiabatic index γ ($\gamma = 5/3$ or 2 or something else). 1.1 is an empirical number. (Spreiter et al., 1966).

Factors Controlling the Standoff Distance

- It is a bit more complicated in MHD and kinetic codes
- Have to consider size and shape of the magnetosphere (depends on pressure and IMF B_z), solar wind M_A and M_S , the spiral/radial IMF orientation, and maybe more (e. g. Cairns & Lyon, 1996)...
- **Let's identify R_{BS} and R_{MP} to determine whether 1.1 is a good empirical coefficient and the appropriate value for γ**

Simulated Magnetosheath Calculations are Easy to Understand

- Simulation



$$R_{MP} = 10.00 R_E$$

$$R_{BS} = 12.833 R_E$$

$$N_{SHEATH} = 22.5 \text{ cm}^{-3}$$

$$N_{SW} = 6.25 \text{ cm}^{-3}$$

$$V_{SW} = 400 \text{ km s}^{-1}$$

$$V_{SHEATH} = 114 \text{ km s}^{-1}$$

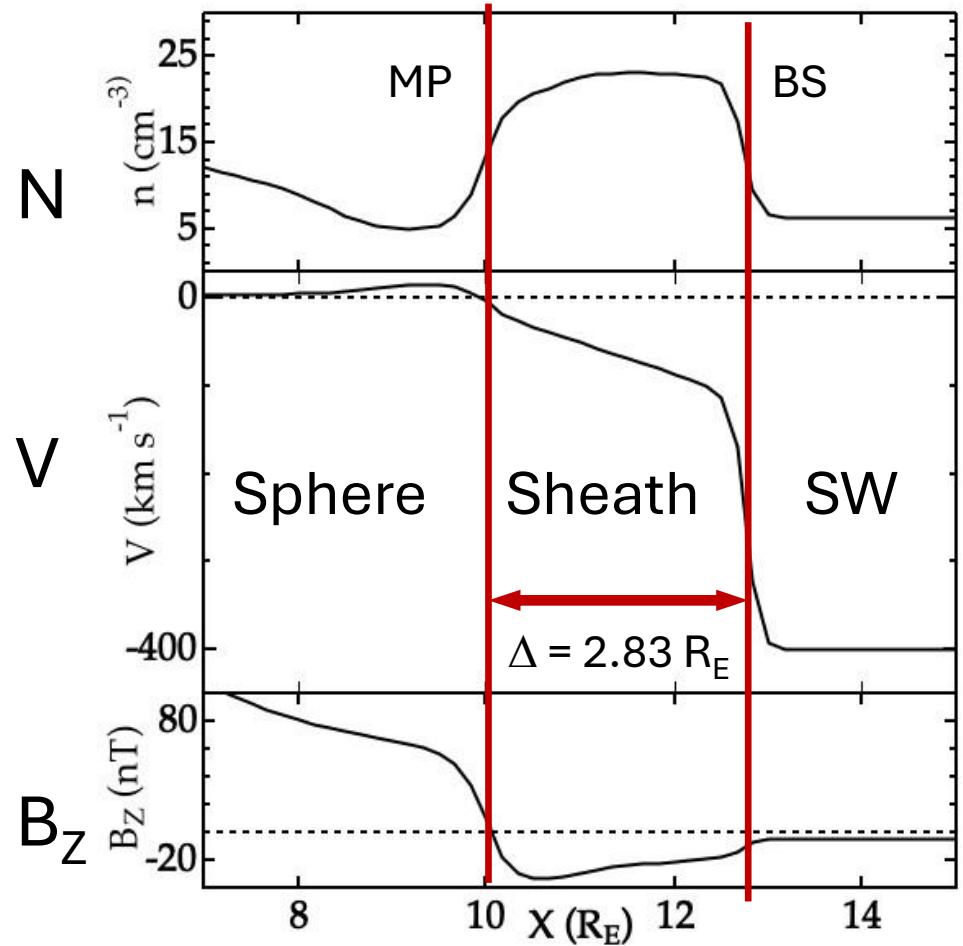
$$\Delta = 2.83 R_E$$

$$1.1 * R_{MP} * N_{SW} / N_{SHEATH} = 3.05 R_E$$

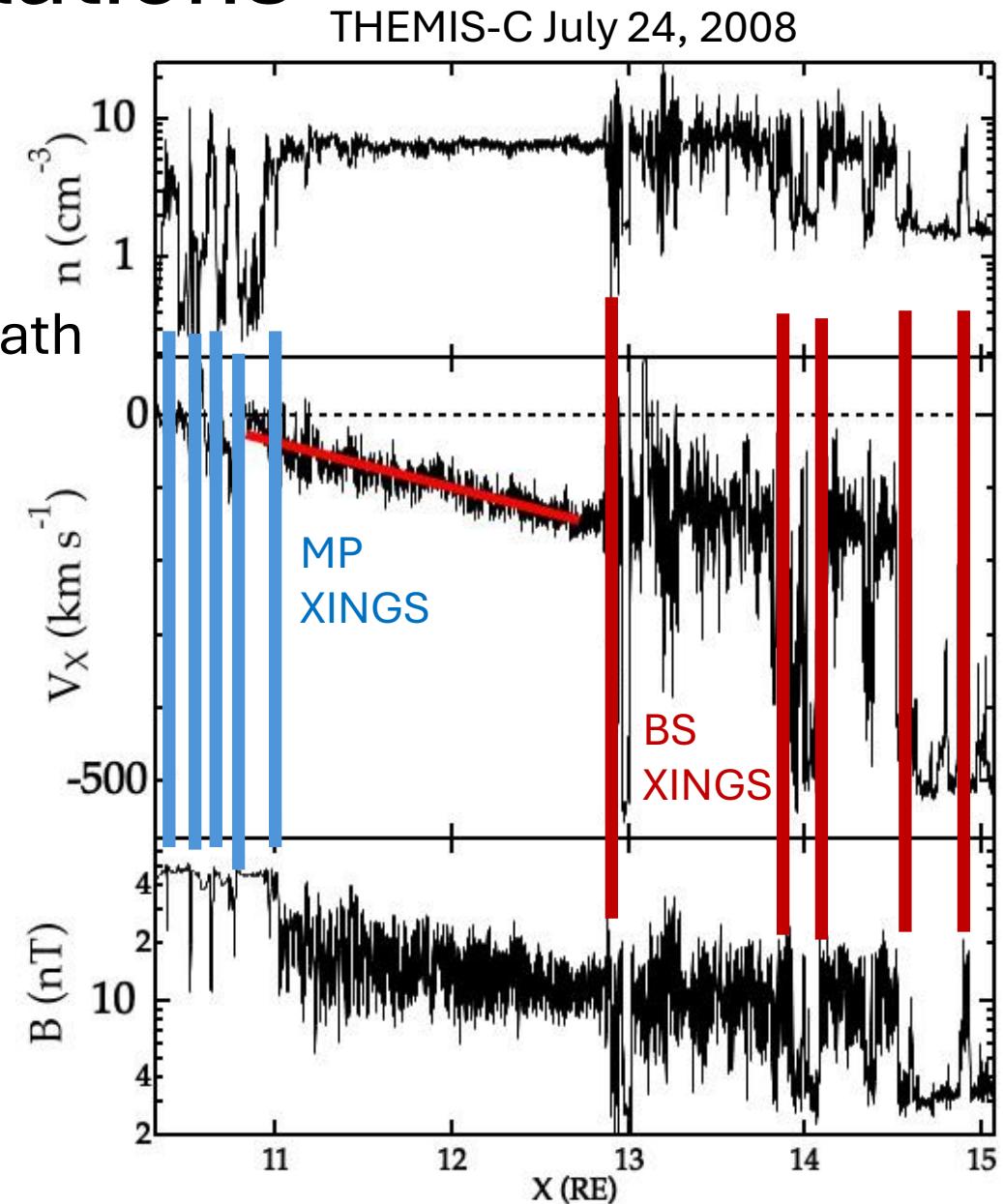
$$1.1 * R_{MP} * V_{SHEATH} / V_{SW} = 3.14 R_E$$

Real Magnetosheath Calculations are Harder

- Simulation



BATS-R-US at CCMC



Empirical Studies of Bow Shock and Magnetopause Locations Define γ

- Where does all the scatter come from?
 - Uncertainties in solar wind measurements
 - Timing, spatial scale lengths, helium content
 - Crossings never occur in equilibrium
(changing solar wind conditions cause boundaries to move past spacecraft, not vice-versa).

Farris and Russell (1991) have a study based on fit BS and MP positions

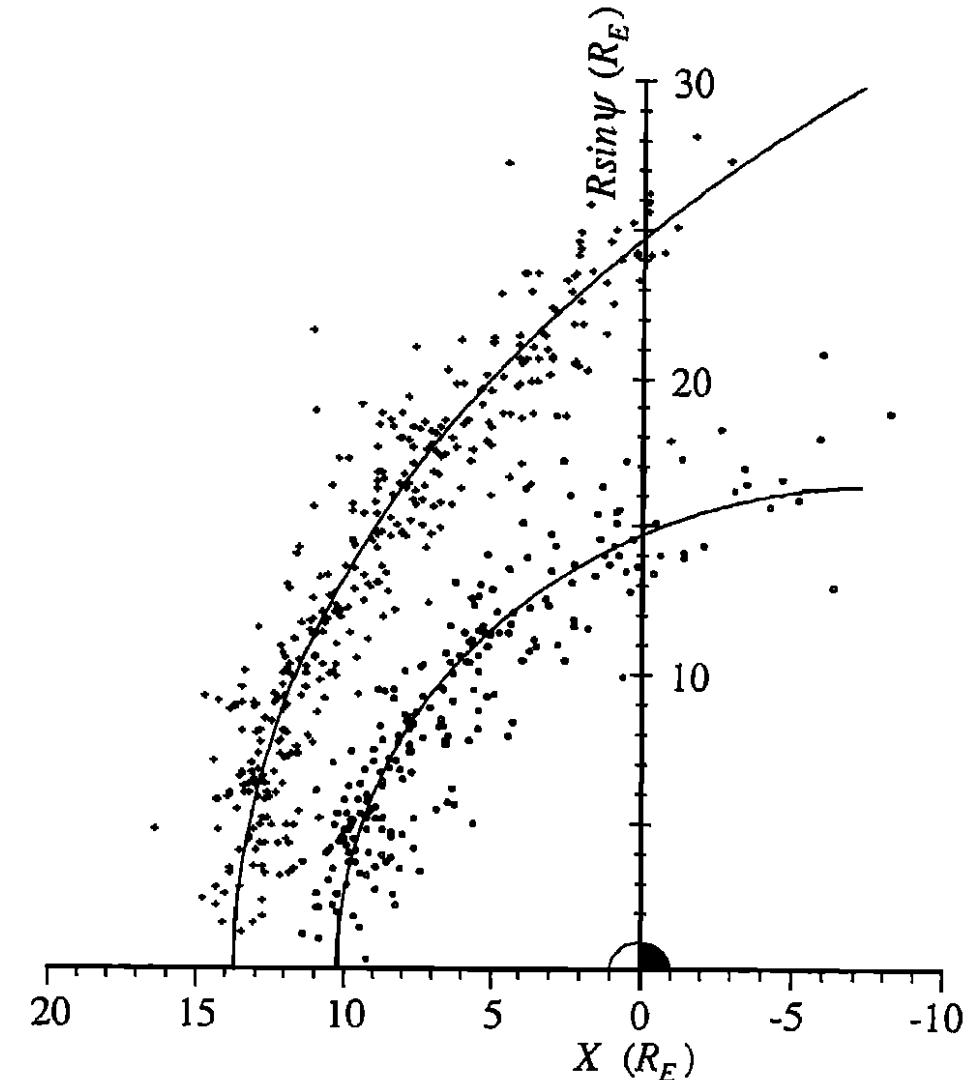
$$R_{\text{BS}} = 13.7 R_E,$$

$$R_{\text{MP}} = 10.3 R_E,$$

$$\Delta = 3.4 R_E$$

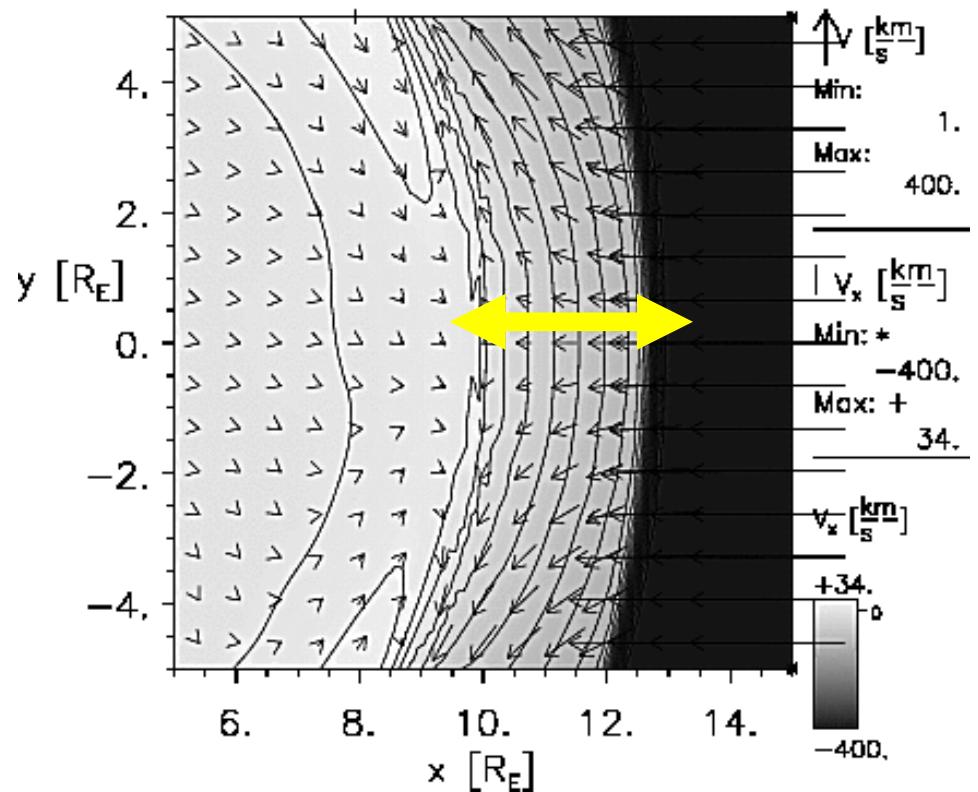
$$n_{\text{SW}}/n_{\text{SHEATH}} = V_{\text{SHEATH}}/V_{\text{SW}} = 0.33$$

$$\gamma = 1.76$$



A New Method Employing the Linear Radial Gradient in Subsolar Velocity V_x

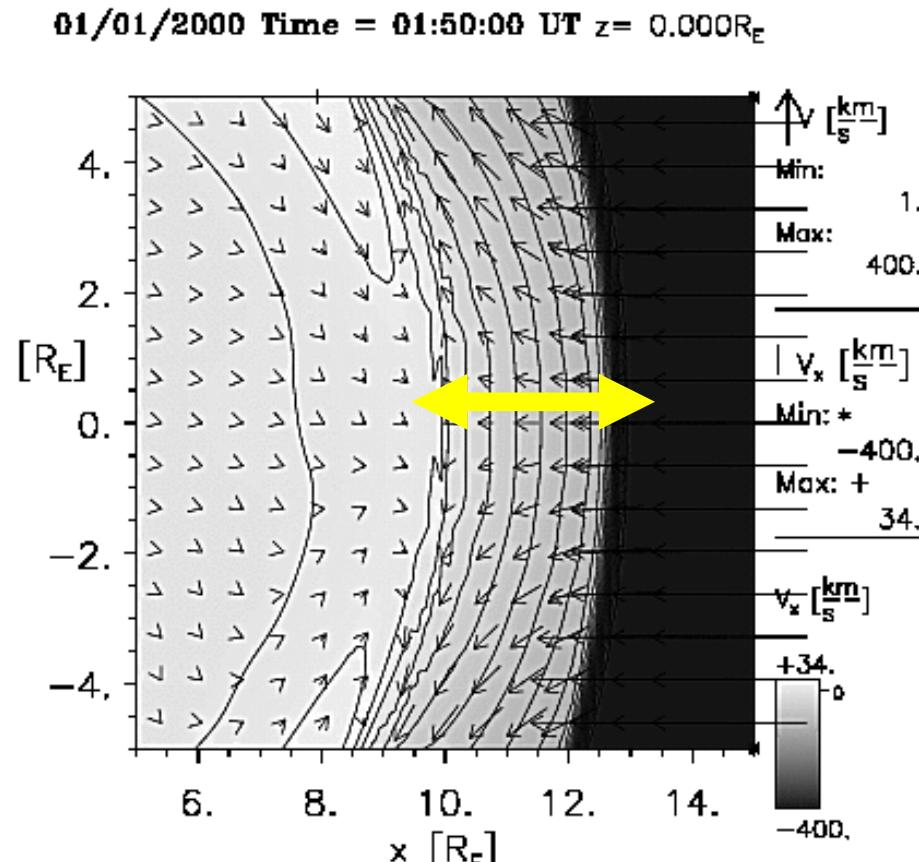
01/01/2000 Time = 01:50:00 UT $z = 0.000R_E$



Model at CCMC; BATSRUS

BATS-R-US at CCMC

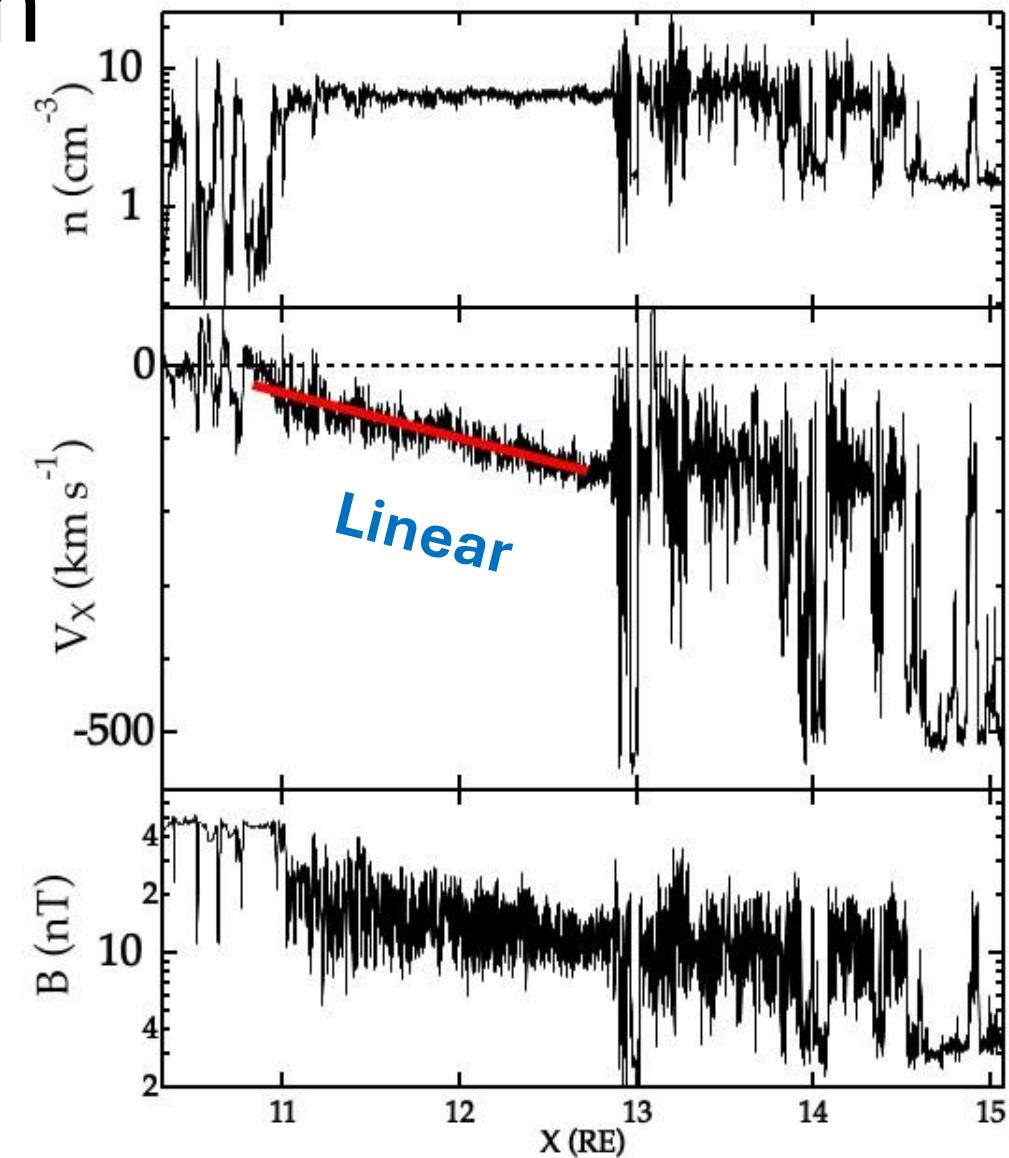
Observations Confirm Linear Gradient in V_x across Subsolar Sheath



Model at CCMC; BATSRUS

BATS-R-US at CCMC

THEMIS-C July 24, 2008

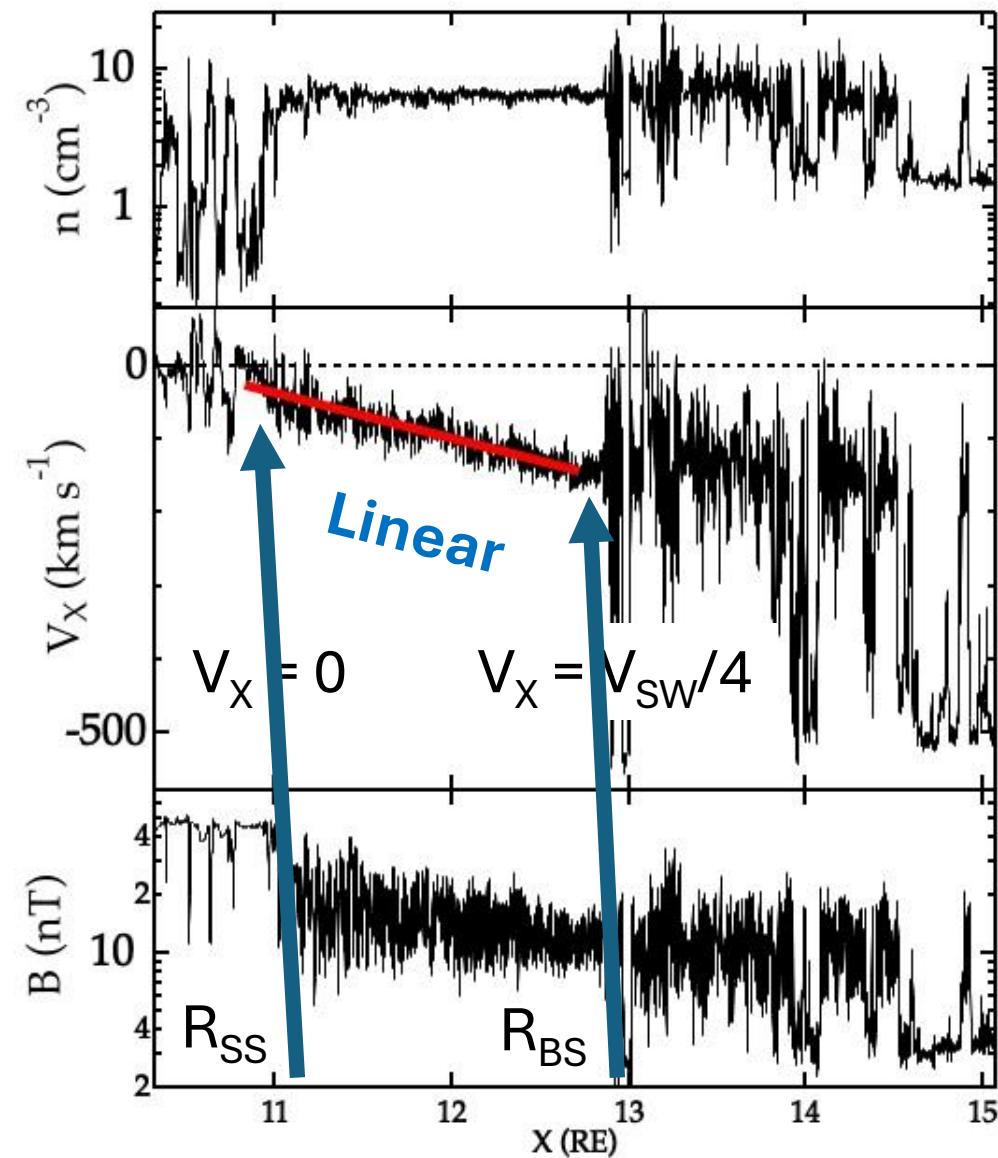


Our Plan

- 1. Fit line to gradient
- 2. Extend to find
 - R_{MP} Subsolar magnetopause, where $V_x = 0$
 - R_{BS} Subsolar bow shock, where $V_x = V_{SW}/4$
- 3. Then simultaneously
- 4. Check $\Delta = 1.1 R_{MP} * V_{SHEATH}/V_{SW}$ and
- 5. Calculate $\gamma = \frac{(1.1 + \Delta/R_{MP}) M_{MS}^2 - 2.2}{(1.1 - \Delta/R_{MP}) M_{MS}^2}$

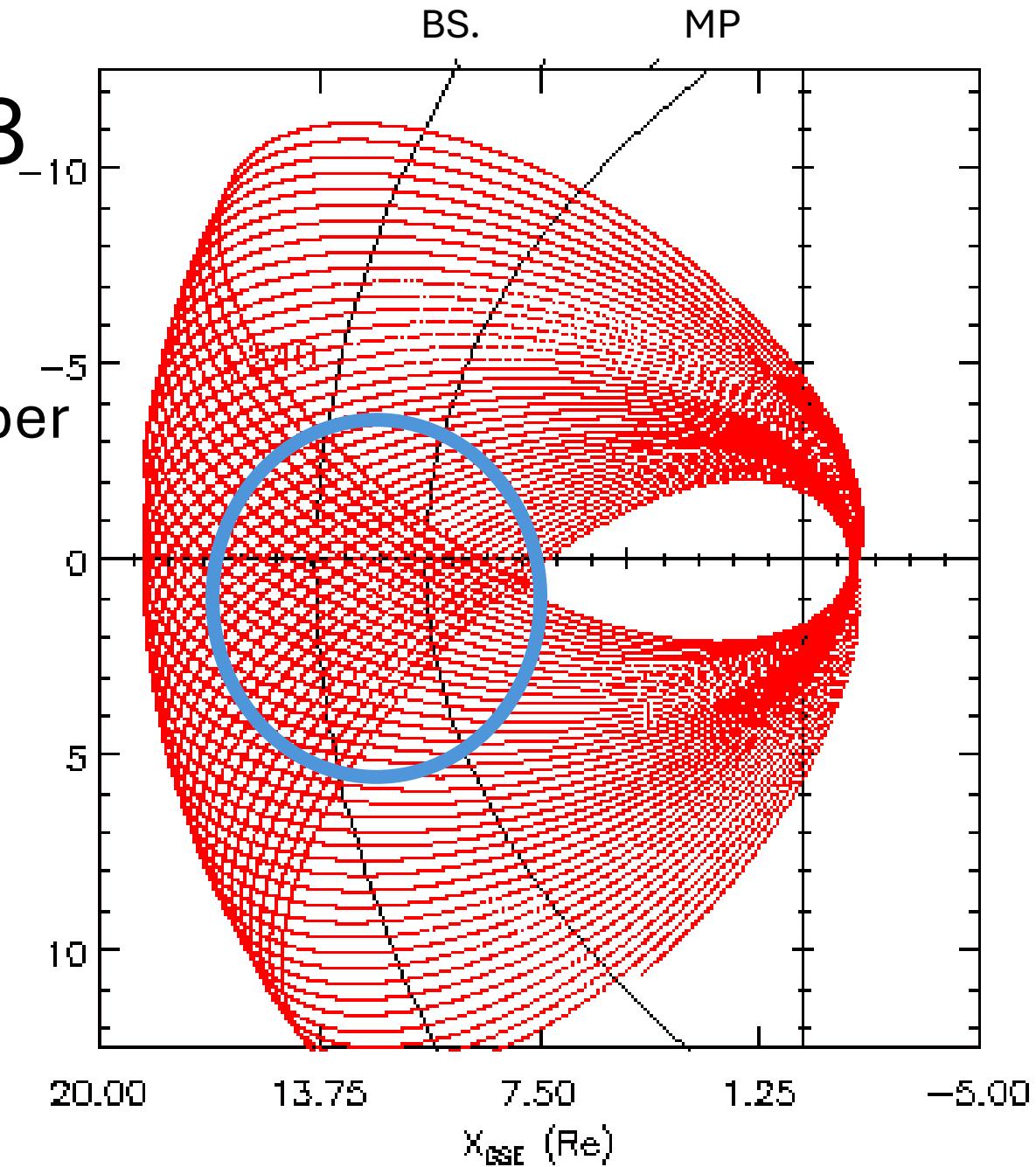
→ Basically $\gamma \sim \Delta$

THEMIS-C July 24, 2008

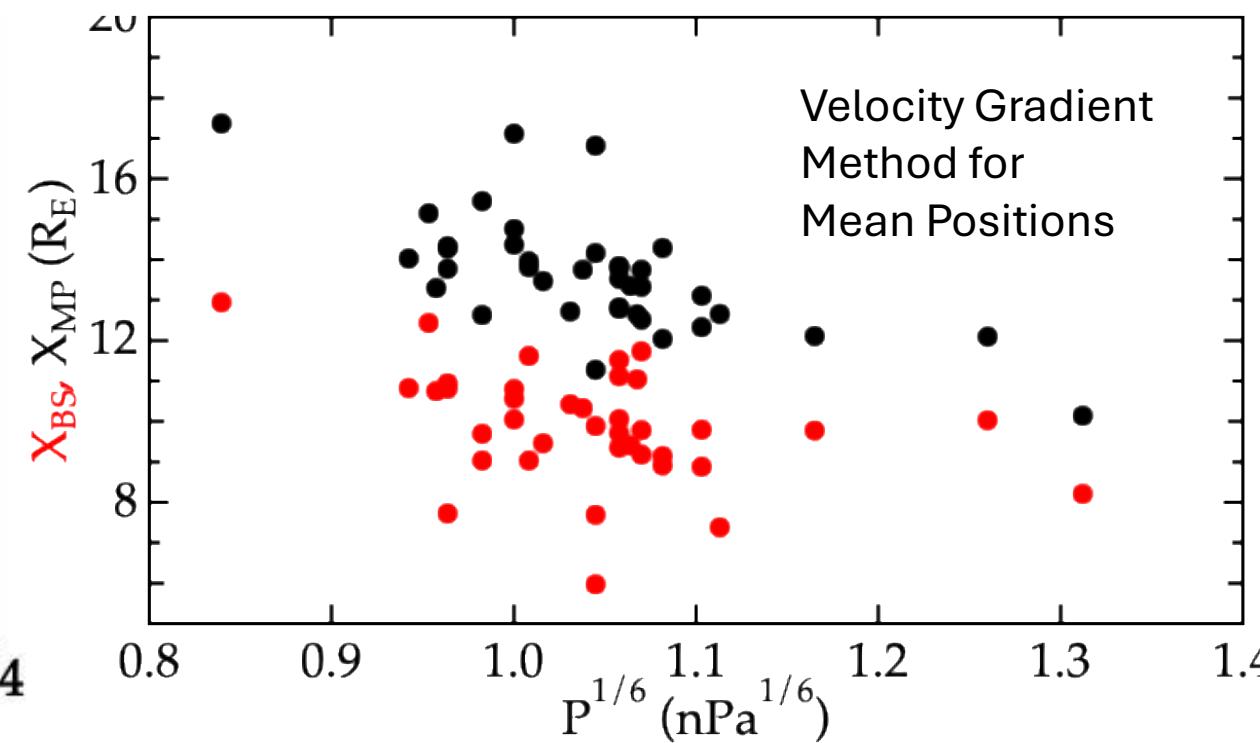
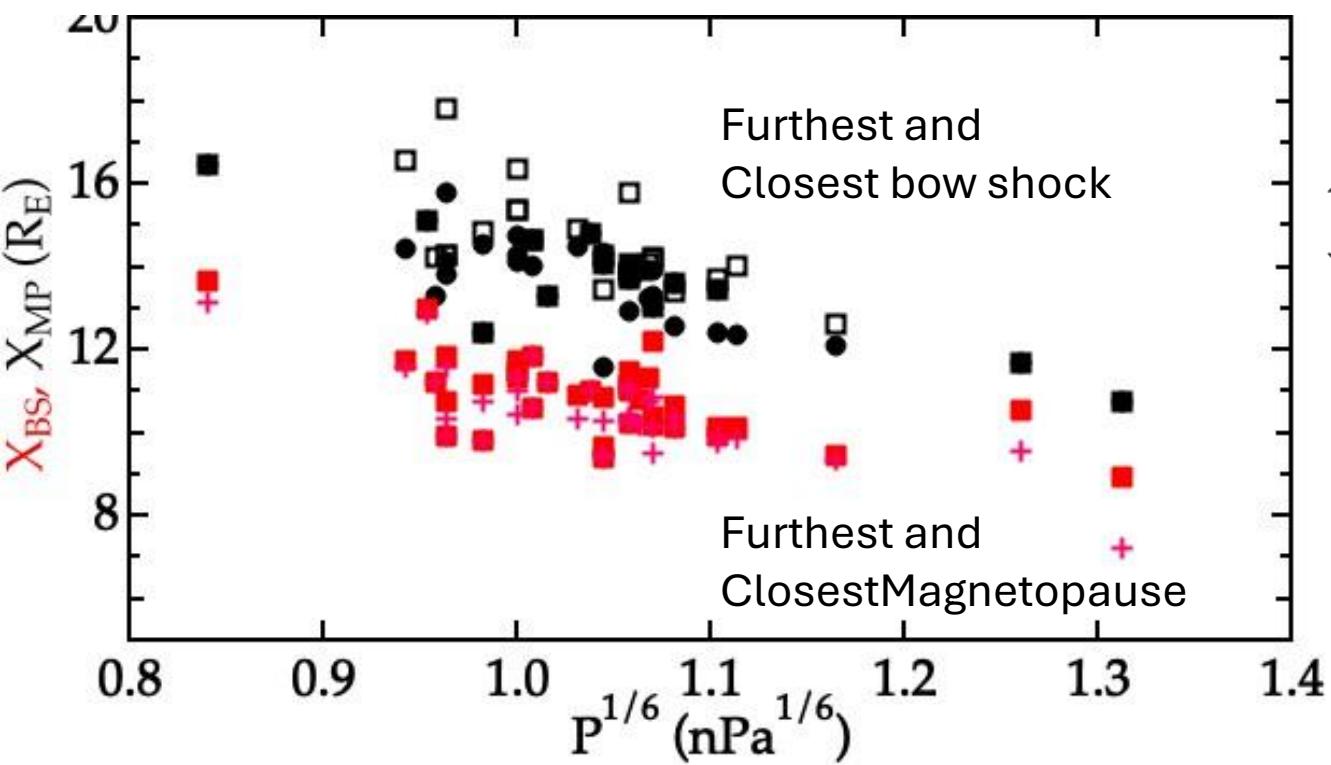


THEMIS-C Orbits in 2008

- Select passes through subsolar magnetosheath, July-September



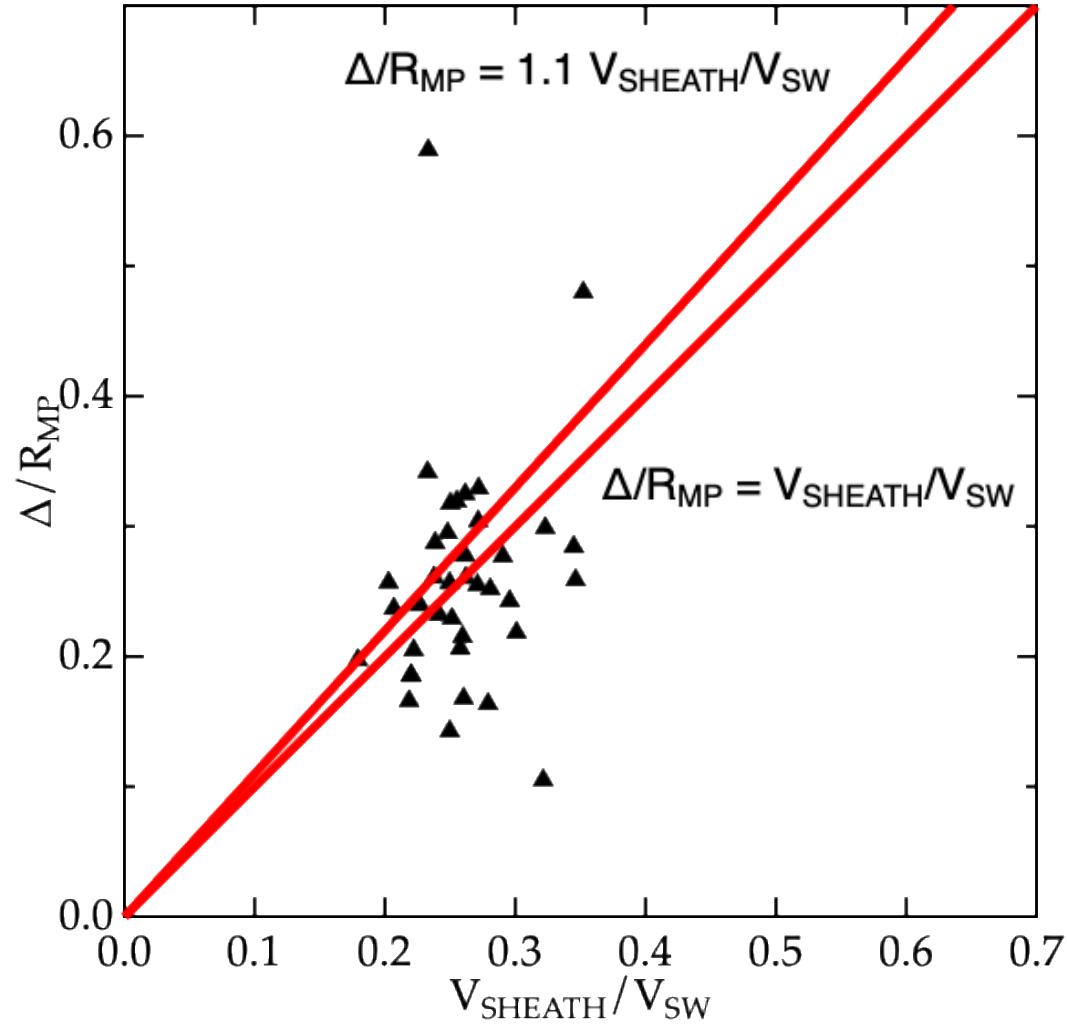
Boundaries Move Earthward as Solar Wind Dynamic Pressure Increases



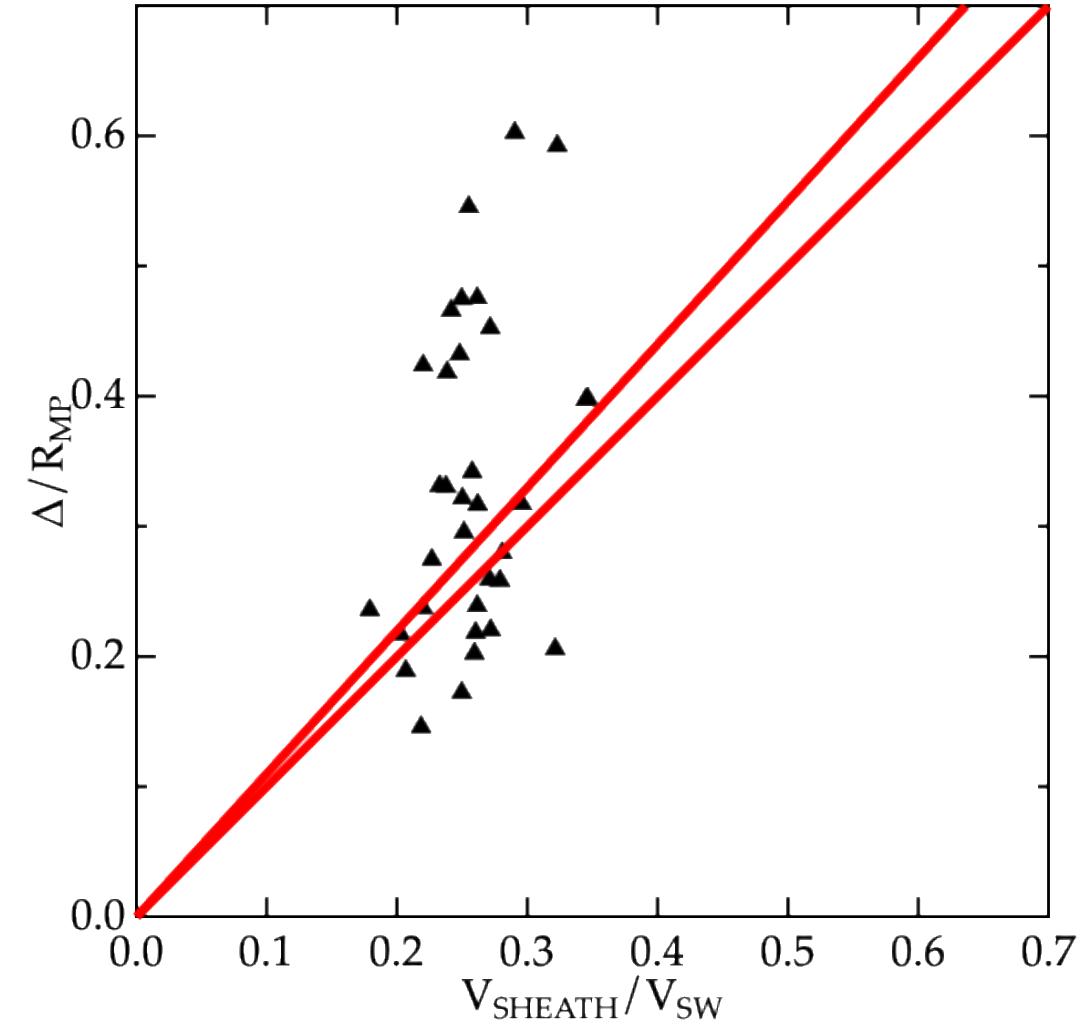
Solar Wind Dynamic Pressure

Does Stand-off Distance Depend on Velocity Jump at Bow Shock?

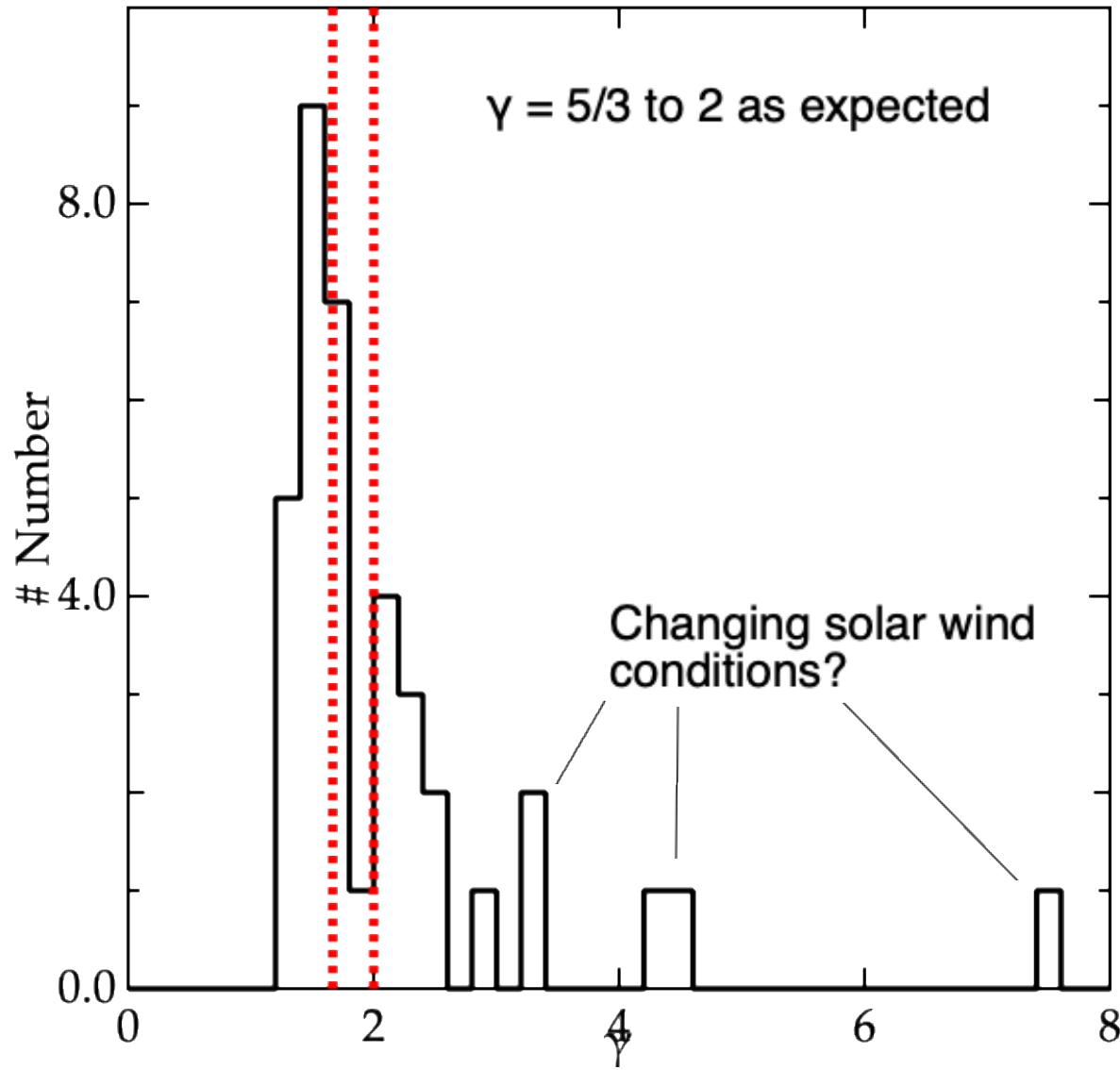
Closest Bow Shock, Furthest Magnetopause



Velocity Gradient Method



Histogram of γ



Summary

- A variety of factors control the locations of the bow shock and magnetopause.
- The same is true for the standoff distance between these boundaries
- Linear velocity gradients mean we can estimate simultaneous bow shock and magnetopause locations, and the stand-off distance between them for steady conditions.
- Preliminary results indicate that the ratio of specific heats in the solar wind is on the order of ~ 1.66 ($=5/3$) to ~ 2.00 . More work needed. ☺